

# วงจรกรองความถี่แบบ KHN ในโหมดกระแสด้วย VDTA เพียงตัวเดียว Current-mode KHN Filter Using Single VDTA

วุฒิพงษ์ พิษิตวงศ์<sup>1</sup>, ชิตสิรร์ วิชิต<sup>1</sup>, ศุภวัฒน์ ลาวัญย์วิสุทธิ์<sup>2</sup>

Received: December, 2013; Accepted: May, 2014

## บทคัดย่อ

บทความนี้นำเสนอวงจรกรองความถี่แบบ KHN โหมดกระแสที่สามารถให้ผลตอบสนองได้ 3 แบบ ในวงจรเดียวกัน ได้แก่ กรองความถี่ต่ำผ่าน สูงผ่าน และแถบความถี่ผ่าน ด้วยอุปกรณ์วงจรขยายผลต่างแรงดันส่งผ่านความนำกระแส (VDTA) เพียงตัวเดียว มีลักษณะเด่นของวงจร คือ สามารถปรับค่าความถี่โพลและค่าควอลิตี้แฟกเตอร์ได้ด้วยวิธีทางอิเล็กทรอนิกส์โดยการปรับกระแส  $I_B$  ได้อย่างอิสระ โครงสร้างของวงจรไม่ซับซ้อนประกอบไปด้วย VDTA เพียง 1 ตัว ร่วมกับตัวเก็บประจุที่ต่อลงกราวด์อีก 2 ตัว ปราศจากตัวต้านทานและใช้กับอุปกรณ์พาสซีสแบบต่อลงกราวด์ วงจรที่นำเสนอนี้ สามารถนำไปพัฒนาเป็นวงจรรวม ผลการจำลองการทำงานของวงจรโดยใช้โปรแกรม PSpice พบว่าให้ผลสอดคล้องกับที่คาดการณ์ไว้ตามทฤษฎี วงจรมีอัตราดิ้งกำลังงาน 1.76mW ที่แหล่งจ่ายไฟฟ้า  $\pm 1.5V$

คำสำคัญ : วงจรกรองความถี่แบบ KHN; วงจรขยายผลต่างแรงดันส่งผ่านความนำกระแส (VDTA)

<sup>1</sup> คณะวิศวกรรมศาสตร์และสถาปัตยกรรมศาสตร์ มหาวิทยาลัยเทคโนโลยีราชมงคลธัญบุรี นครราชสีมา

<sup>2</sup> คณะเทคโนโลยีอุตสาหกรรม มหาวิทยาลัยราชภัฏเทพสตรี

E - mail : wudthipong@hotmail.com, ch\_wichito@hotmail.com, s.lawanwisut@hotmail.com

## Abstract

This article presents a current-mode KHN universal biquadratic filter performing 3 standard functions at the same time: low-pass, high-pass and band-pass functions, based on only a single voltage difference transconductance amplifier (VDTA). The features of the circuit are that: the pole frequency and quality factor can be electronically tuned via the input bias currents  $I_b$ . The circuit topology is very simple, consisting of merely single VDTA and 2 grounded capacitors. Without any external resistor and using only grounded elements, the proposed circuit is very suitable to further develop into an integrated circuit. The PSpice simulation results are shown. The given results agree well with the theoretical anticipation. The maximum power consumption is approximately 1.76mW at  $\pm 1.5V$  power supply voltages.

**Keywords :** KHN filter; VDTA

## Introduction

An analog filter is an important building block, widely used for continuous-time signal processing. It can be found in many fields: including communications, measurement, instrumentation and control systems (Sedra and Smith, 2003; Ibrahim et al., 2005). One of the most popular analog filters is the multifunction filter, since it can provide several functions at the same time. It has been accepted that the Kerwin—Huelsman—Newcomb (KHN) biquad filter is also the more popular multifunction filter structure. Because this structure offers several advantages such as low passive and active sensitivity performance, low component spread and good stability behavior (Kerwin et al., 1998; Deliyannis et al., 1999). The KHN filters have been realized by employing different high performance active building blocks. The voltage-mode KHN filters based on CCIIs (Soliman, 1994; Senan and Singh, 1995), CDBAs (Khaled and Soliman, 2000), DVCC (Minnae and Ibrahim, 2008), DDCC (Ibrahim and Kuntman, 2004), VDTA (Satansup et al., 2013) and op-amps have been developed. These reported circuits provide good performances but they suffer from some disadvantages for example, excessive use of the passive elements especially external resistors, lack of electronic adjustability, limitation at high frequency performance due to gain-bandwidth of op-amp. The CCCII

(Altuntas and Toker, 2002) and OTA (Shah and Bhaskar, 2002) based voltage-mode KHN filter enjoy electronic tunability. Unfortunately, the circuit (Shah and Bhaskar, 2002) requires the use of large number of CCCIs (5 CCCIs). Moreover, the OTA-based circuitries known to be restrained by limited operating range and output voltage swing. Recently, the multifunction filters working in current-mode have been more popularly used than the voltage-mode type. Since the last decade, there has been much effort to reduce the supply voltage of analog systems. This is due to the demand for portable and battery-powered equipment. Since a low voltage operating circuit becomes necessary, the current-mode technique is ideally suited for this purpose. Actually, a circuit using the current-mode technique has many other advantages, such as, larger dynamic range, higher signal bandwidth, greater linearity, simpler circuitry and lower power consumption (Toumazou et al., 1990). The current-mode KHN filter based on different high performance current-mode active components are reported in literature (Altuntas and Toker, 2002; Toker et al., 1999; Keskin et al., 2006; Biolek et al., 2007). However, some of these circuits require more active elements which make the circuit becoming more complicated and consumes more power.

Therefore, the aim of this paper is to propose a single active element based CM resistorless universal filter. For this purpose, the voltage differencing transconductance amplifier (VDTA) (Biolek et al., 2008) is a recently introduced active element. The VDTA device is composed of current source controlled by the difference of two input voltages and a multiple-output transconductance amplifier, providing electronically controlled ability through its transconductance gains. Therefore, the VDTA device is very suitable for electronically tunable active circuit synthesis. Another advantage feature of the use of the VDTA as an active element is that compact structures in some application can be achieved easily (Biolek et al., 2008).

The aim of this paper is to propose a current-mode KHN filter, emphasizing on use of single VDTA and grounded capacitors. The features of the proposed circuit are as follows: It can provide 3 transfer functions such as low-pass, high-pass and band-pass without changing the circuit topology. The circuit configuration is very simple, employing only grounded capacitors as passive components, thus it is suitable for fabricating in monolithic chip. The quality factor and pole frequency can be electronically adjusted.

## Circuit Principle

### Description of the VDTA

In 2008, the conceptual of the VDTA was firstly suggested by Biolek (Biolek et al., 2008) The schematic symbol of the VDTA is represented in figure 1, where the port relations can be defined by the following expression (Yesil et al., 2011).

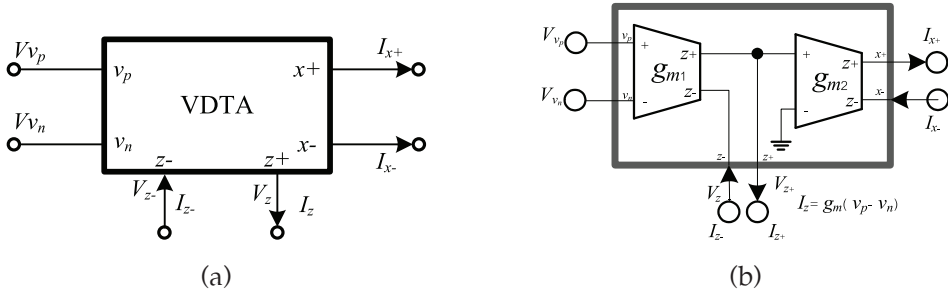


Figure 1. (a) Symbol of the VDTA and (b) its implement by OTAs.

$$\begin{bmatrix} I_z \\ I_{x+} \\ I_{x-} \end{bmatrix} = \begin{bmatrix} g_{m1} & -g_{m1} & 0 \\ 0 & 0 & g_{m2} \\ 0 & 0 & g_{m2} \end{bmatrix} \begin{bmatrix} V_p \\ V_n \\ V_z \end{bmatrix} \quad (1)$$

In equation (1),  $g_{m1}$  and  $g_{m2}$  are the first and second transconductance gains of the VDTA respectively. The differential input voltage from the terminals  $p$  and  $n$  ( $V_p - V_n$ ) is transformed into output currents at the terminals  $z$  and  $z-$  with first transconductance  $g_{m1}$ . The voltage drop at the terminal  $z$  ( $V_z$ ) is transformed into output currents at the terminals  $x+$  and  $x-$  with second transconductance  $g_{m2}$ . For a BJT VDTA, the  $g_m$  can be expressed as

$$g_m = \frac{I_B}{2V_T} \quad (2)$$

where  $I_B$  and  $V_T$  are the bias current and the thermal voltage ( $V_T$ ), respectively. Generally, VDTA can contain an arbitrary number of  $x$  terminals, providing currents  $I_B$  of both directions. In the same way, the number of  $z$  terminals can be arbitrarily included by using the internal current mirror to provide a copy of the current flowing out of the  $z$  terminal to the other  $z$  terminals (called  $z_c$  terminal). As an example, the symbol of the VDTA with a pair of  $x+$ ,  $x-$ ,  $z$  and  $z-$  terminals are illustrated in figure 1, respectively.

### General structure of KHN biquad filter

A KHN structure consists of two integrator blocks and a summer block as shown in figure 2. From block diagram in figure 2, the transfer functions of HP, BP and LP can be respectively expressed as follows:

$$HP(s) = \frac{s^2}{s^2 + s \frac{1}{\tau_1} + \frac{1}{\tau_1 \tau_2}}, \quad (3)$$

$$BP(s) = \frac{s \frac{1}{\tau_1}}{s^2 + s \frac{1}{\tau_1} + \frac{1}{\tau_1 \tau_2}}, \quad (4)$$

$$LP(s) = \frac{\frac{1}{\tau_1 \tau_2}}{s^2 + s \frac{1}{\tau_1} + \frac{1}{\tau_1 \tau_2}}. \quad (5)$$

The pole frequency and quality factor can be expressed as

$$\omega_o = \sqrt{\frac{1}{\tau_1 \tau_2}} \quad (6)$$

and

$$Q_o = \sqrt{\frac{\tau_1}{\tau_2}}. \quad (7)$$

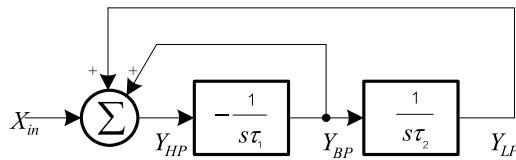


Figure 2. Fundamental KHN structure.

### The proposed current-mode KHN filter

As mentioned in the last section, the proposed KHN filter is based on current summer and lossless integrators. In this section, these circuits will be described. The current summer based on VDTA is shown in figure 3. The output current of this circuit can be written as

$$I_O = I_{x+} = I_1 + I_2 + I_3 \quad (8)$$

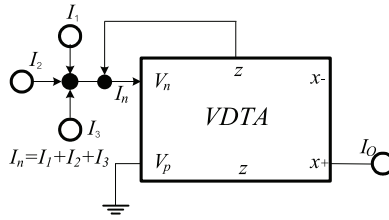


Figure 3. Current summer.

Figure 4 shows the lossless integrator employing VDTA. Considering the circuit figure 4 (a) and (b) using VDTA properties, we will receive

$$\tau_1 = \frac{g_{m1}}{sC_1} \quad (9)$$

and

$$\tau_2 = \frac{g_{m2}}{sC_2} \quad (10)$$

where  $\tau$  is the time constant.

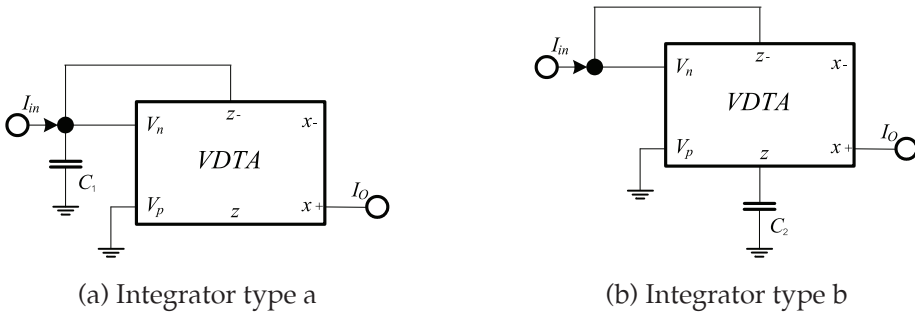


Figure 4. Lossless integrator employing VDTA.

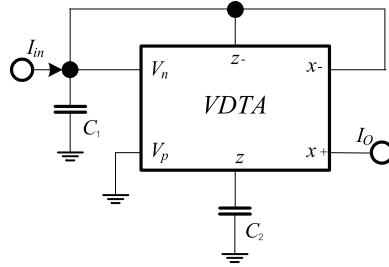


Figure 5. The proposed current-mode KHN filter.

As mentioned in the above section, the proposed KHN filter is based on two integrator blocks and a summer block. The operation of this filter can be achieved very conveniently with the combination of figure 3 and figure 4 together. As can be seen, this topology can be realized using a single VDTA and two grounded capacitors as shown in figure 5. The current transfer functions can be obtained as follows:

$$HP(s) = \frac{I_{HP}(s)}{I_{in}(s)} = \frac{s^2}{s^2 + s \frac{g_{m1}}{C_1} + \frac{g_{m1}g_{m2}}{C_1C_2}}, \quad (11)$$

$$BP(s) = \frac{I_{BP}(s)}{I_{in}(s)} = \frac{s \frac{g_{m1}}{C_1}}{s^2 + s \frac{g_{m1}}{C_1} + \frac{g_{m1}g_{m2}}{C_1C_2}}, \quad (12)$$

$$LP(s) = \frac{I_{LP}(s)}{I_{in}(s)} = \frac{\frac{g_{m1}g_{m2}}{C_1C_2}}{s^2 + s \frac{g_{m1}}{C_1} + \frac{g_{m1}g_{m2}}{C_1C_2}}, \quad (13)$$

from equations (11)-(13), the pole frequency and quality factor can be expressed as

$$\omega_o = \sqrt{\frac{g_{m1}g_{m2}}{C_1C_2}} \quad (14)$$

$$Q_o = \sqrt{\frac{g_{m2}C_1}{g_{m1}C_2}}. \quad (15)$$

Substituting the intrinsic resistance and transconductance as depicted in equations (9) and (10) into equations (14) and (15), it yields pole frequency and quality factor as follows:

$$\omega_o = \frac{1}{2V_T} \sqrt{\frac{I_{B1}I_{B2}}{C_1C_2}} \quad (16)$$

and

$$Q_o = \sqrt{\frac{C_1I_{B2}}{C_2I_{B1}}} \quad (17)$$

from equations (16) and (17), by maintaining the ratio  $I_{B1}$  and  $I_{B2}$  to be constant, it can be remarked that the pole frequency can be adjusted by varying  $I_{B1}$  and  $I_{B2}$  without affecting the quality factor. Moreover, the circuit can provide high  $Q_o$  by setting value of  $C_1$  more than value of  $C_2$ . The filter bandwidth (BW) can be expressed as follows:

$$BW = \frac{\omega_o}{Q_o} = \frac{2V_T I_{B1}}{C_1} \quad (18)$$

Note that the bandwidth can be linearly controlled by  $I_{B1}$ .

### Tracking Errors and Sensitivity Analysis

Considering the non-ideal characteristics of VDTA, the relation of current and voltage in equation (1) can be rewritten as:

$$\begin{bmatrix} I_z \\ I_{x+} \\ I_{x-} \end{bmatrix} = \begin{bmatrix} \beta_1 g_{m1} & -\beta_1 g_{m1} & 0 \\ 0 & 0 & \beta_2 g_{m2} \\ 0 & 0 & -\beta_2 g_{m2} \end{bmatrix} \begin{bmatrix} V_{V_p} \\ V_{V_n} \\ V_z \end{bmatrix} \quad (19)$$

where  $\beta_1$  and  $\beta_2$  are the tracking errors for the first and second stages of the VDTA respectively. Reanalysis of the proposed circuit in figure 5 employing equation (19) yields the following non-ideal filter parameters.

$$\omega_o = \sqrt{\frac{\beta_1 \beta_2 g_{m1} g_{m2}}{C_1 C_2}} \quad (20)$$

and



$$Q_o = \sqrt{\frac{\beta_2 g_{m2} C_1}{\beta_1 g_{m1} C_2}}. \quad (21)$$

It is evident that the values of  $\omega_o$  and  $Q$  may be slightly changed by the effect of the VDTA tracking errors. However, the small deviation in equations (20) and (21) can be minimized by properly adjusting the VDTA transconductance values. Hence, the desired parameter values can still be satisfied.

The sensitivities of the proposed circuit can be found as

$$\begin{aligned} S_{I_{B1}}^{\omega_o} &= S_{I_{B2}}^{\omega_o} = \frac{1}{2}, \\ S_{C_1}^{\omega_o} &= S_{C_2}^{\omega_o} = -\frac{1}{2}, \\ S_{V_T}^{\omega_o} &= \frac{1}{2} \end{aligned} \quad (22)$$

and

$$\begin{aligned} S_{I_{B2}}^{Q_o} &= S_{C_1}^{Q_o} = \frac{1}{2}, \\ S_{I_{B1}}^{Q_o} &= S_{C_2}^{Q_o} = -\frac{1}{2}. \end{aligned} \quad (23)$$

Therefore, all the active and passive sensitivities are equal or less than unity in magnitude.

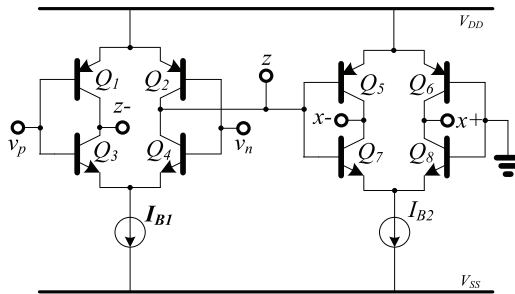


Figure 6. Internal construction of VDTA

## Results

To prove the performances of the proposed filter, a PSpice simulation was carried out. The PNP and NPN transistors employed in the proposed circuit were simulated by respectively using the parameters of the PR200N and NR200N bipolar transistors of ALA400 transistor array from AT&T (Frey, 1993). Figure 4 depicts schematic description of the VDTA used in the simulations. The circuit was biased with  $\pm 1.5V$  supply voltages. The circuit was connected to a  $1\Omega$  load resistor.  $C1=C2=1nF$  and  $I_{B1}=50\mu A$  and  $I_{B2}=150\mu A$  are chosen. It yields the pole frequency of 198.39kHz. The results shown in figure 5 are the gain responses of the proposed KHN biquad filter. It clearly shows that this circuit can provide simultaneously low-pass, high-pass and band-pass responses without modifying the circuit topology. Figure 6 displays gain responses of band-pass function with different  $I_B$  values. It is shown that the bandwidth of the responses can be adjusted by the input bias current  $I_B$ , figure 7 shows gain responses of band-pass function where  $I_{B1}$  and  $I_{B2}$  are equally set to keep the ratio to be constant and changed for several values. It is found that pole frequency can be adjusted without affecting the quality factor.

In order to investigate a time-domain response of the proposed current-mode universal filter, a 198.39kHz sinusoidal input current of 20mA is applied to the filter. The results obtained are shown comparing input and output waveforms of the LP, HP and BP responses in figure 8. (a), (b) and (c) respectively. It can be seen from simulations that in case of BP response, the total harmonic distortion (THD) of about 1.61% approximately at the total power consumption of 1.76mW can be obtained.

## Conclusion

A current-mode KHN biquad filter based on single VDTA has been presented. The features of the proposed circuit are that: pole frequency and quality factor can be electronically adjusted via input bias currents. The circuit description comprises only single VDTA and 2 grounded capacitors. With mentioned features, it is very suitable to realize the proposed circuit in monolithic chip to use in battery powered, portable electronics equipment such as wireless communication system devices.

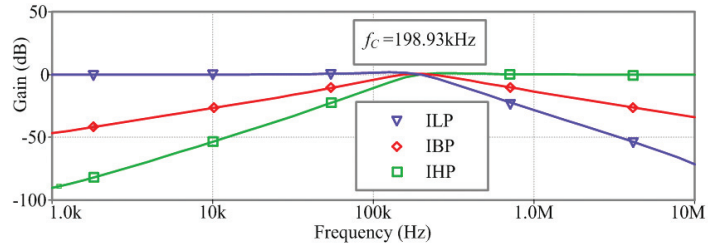


Figure 7. Gain responses of the proposed circuit

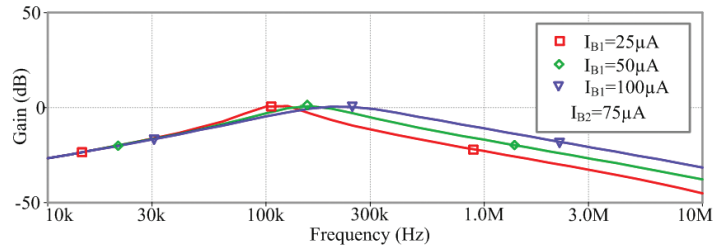


Figure 8. Band-pass responses for different values  $I_{B1}$

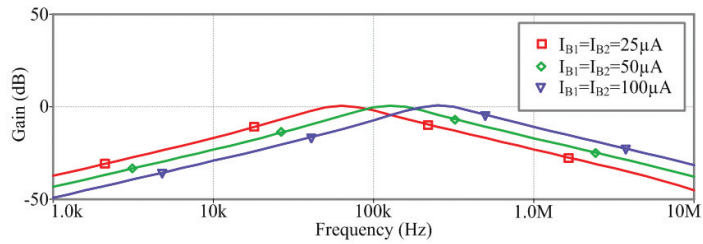
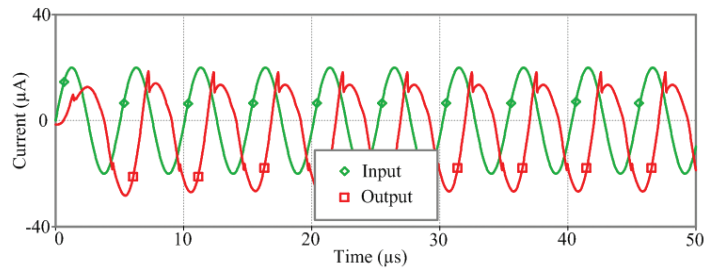
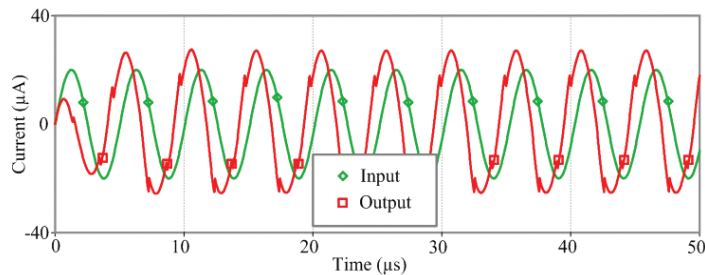


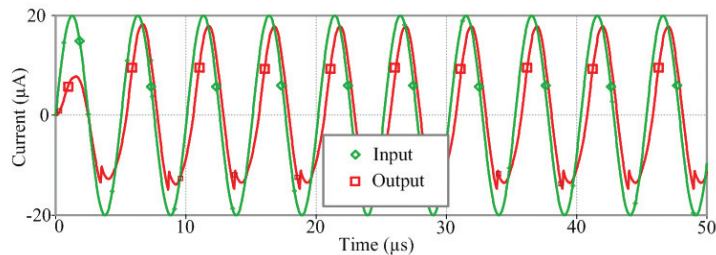
Figure 9. Band-pass responses for different values of  $I_{B1}$  and  $I_{B2}$  with keeping their ratios constant



(a) LP



(b) HP



(c) BP

Figure 10. Input and output waveforms of the LP, HP and BP responses for a 198.39kHz sinusoidal input current of 20mA

## References

- Altuntas E. and Toker A. (2002). Realization of voltage and current mode KHN biquads using CCCII. *International Journal of electronics and Communications (AEU)*. vol.59. pp.45-49.
- Biolek D., Senani R., Biolkova V. and Kolka Z. (2008). Active elements for analog signal processing: Classification, review, and new proposals. *Radioengineering*. vol.17. no. 4. pp.15-32.

- Deliyannis T., Sun Y. and Fidler J.K. (1999). Continuous time active filter design. USA: CRC Press.
- Frey D.R., (1993). Log-domain filtering: an approach to current-mode filtering. IEE Proceeding of Circuit Devices Systems. vol.140. pp.406-416.
- Ibrahim M.A. and Kuntman H.A. (2004). A novel high CMRR high input impedance differential voltage-mode KHN-biquad employing DODDCs. International Journal of electronics and Communications (AEU). vol.5. pp.429-433.
- Ibrahim M.A., Minaei S., and Kuntman H.A. (2005). A 22.5MHz current-mode KHN-biquad using differential voltage current conveyor and grounded passive elements. International Journal of electronics and Communications (AEU). vol.59. pp.311-318.
- Kerwin W., Huelsman L., and Newcomb R. (1997). State variable synthesis for insensitive integrated circuit transfer function. IEEE Journal of Solid-State Circuits, SC-2: pp.87-92.
- Khaled N.S., and Soliman A.M. (2000). Voltage mode Kerwin-Huelsman-Newcomb circuit using CDBAs. Frequenz. vol.54. pp.90-93.
- Minae S., and Ibrahim M.A. (2008). A mixed-mode KHN-biquad using DVCC and grounded passive elements suitable for direct cascading. International Journal of Circuit Theory and Applications. online first.
- Satansup J., Pukkalanum T. and Tangsrirat W. (2013). Electronically Tunable Current-Mode Universal Filter Using VDTAs and Grounded Capacitors. Proceeding of the IMECS 2013. vol.2. Hong kong.
- Sedra A.S. and Smith K.C. (2003). Microelectronic circuits. 5<sup>th</sup> edition. Florida: Holt, Rinehart and Winston.
- Senan R., and Singh V.K. (1995). KHN-equivalent biquad using current conveyors. Electronics Letters. vol.31. pp.626-628.
- Shah S., and Bhaskar D.R. (2002). Design of KHN biquad using operational transconductance amplifier. The 45<sup>th</sup> Midwest Symposium Circuits and Systems (MWSCAS-2002). 4-7 Aug. 2002. pp.148-151.
- Soliman A.M. (1994). Kerwin-Huelsman-Newcomb circuit using current conveyors. Electronics Letters. vol.30. pp.2019-2020.
- Toumazou C. Lidgey F.J. and Haigh D.G. (1990). Analogue IC design: the current-mode approach. London: Peter Peregrinus.
- Yesil A., Kacar F., and Kuntman H. (2010). New simple CMOS realization of voltage differencing transconductance amplifier and its RF filter application. Radioengineering 2011. pp.632-637.