



## Achieving Privacy Preservation Constraints based on K-Anonymity in conjunction with Adjacency Matrix and Weighted Graphs

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### ABSTRACT

A well-known privacy preservation model is  $k$ -anonymity. It is simple and widely applied in several real-life systems. To achieve  $k$ -anonymity constraints in datasets, all explicit identifiers of users are removed. Furthermore, the unique quasi-identifiers of users are distorted by their less specific values to be at least  $k$  indistinguishable tuples. For this reason, after datasets are satisfied by  $k$ -anonymity constraints, they can guarantee that all possible query conditions to them always have at least  $k$  tuples that are satisfied. Aside from achieving privacy preservation constraints, the data utility and the complexity of data transformation are serious issues that must also be considered when datasets are released. Therefore, both privacy preservation models are proposed in this work. They are based on  $k$ -anonymity constraints in conjunction with the weighted graph of correlated distortion tuples and the adjacency matrix of tuple distances. The proposed models aim to preserve data privacy in datasets. Moreover, the data utility and data transform complexities are also considered in the privacy preservation constraint of the proposed models. Furthermore, we show that the proposed data transformation technique is more efficient and effective by using extensive experiments.

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### 1. INTRODUCTION

Privacy violation is a serious issue that the data holder must consider when datasets are released to utilize in the outside scope of data-collecting organizations [1], i.e., the data holder must ensure that when the datasets are released, they must not have any concern of privacy violation issues. To achieve these aims in released datasets,  $k$ -anonymity is proposed. An example of privacy preservation is based on  $k$ -anonymity constraints. Let Table 1 be the original dataset such that Age and Gender are the quasi-identifier attributes. Another attribute, Disease, is the sensitive attribute. Suppose the value of  $k$  is 2. In this situation, a released data version of Table 1 is shown in Table 2. Although Table 2 is more secure in terms of privacy preservation than its original data version (Table 1), we can see that it loses some data meaning in terms of data utilization. In addition,  $k$ -anonymity is more complex in terms of data transformation. To rid these vulnerabilities of  $k$ -anonymity,

both privacy preservation models are proposed in this work. They are based on  $k$ -anonymity constraints in conjunction with the weighted graph of correlated distortion tuples and the adjacency matrix of tuple distances.

**Table 1:** An example of original dataset.

#ID	Age	Gender	Disease
$d_1$	45	Male	Flu
$d_2$	46	Female	Fever
$d_3$	47	Male	Cancer
$d_4$	48	Male	HIV
$d_5$	48	Female	Flu
$d_6$	42	Female	HIV
$d_7$	42	Female	Fever

**Table 2:** A 2-Anonymity data version of Table 1.

#ID	Age	Gender	Disease
$d_1$	45 - 48	*	Flu
$d_2$	45 - 48	*	Fever
$d_5$	45 - 48	*	Flu
$d_3$	47 - 48	Male	Cancer
$d_4$	47 - 48	Male	HIV
$d_6$	42	Female	HIV
$d_7$	42	Female	Fever

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The organization of this paper is as follows. In this section, privacy preservation issues and the traditional  $k$ -anonymity are presented. In the next section, we illustrate other existing privacy preservation models, data distortion techniques, and data transformation algorithms for transforming datasets to satisfy privacy preservation constraints. In Section 3, we propose the data distortion techniques for the numerical and non-numeric quasi-identifier, the distance of tuples, and both privacy preservation models that are based on  $k$ -anonymity constraints in conjunction with the weighted graph of correlated distortion tuples and the adjacency matrix of tuple distances. Then, the data utility metrics for evaluating the data utility of released datasets are presented (Section 4). The experimental results can indicate the effectiveness and efficiency of both proposed privacy preservation models. They are discussed in Section 5. Finally, the conclusion of this work will be discussed in Section 6.

## 2. BACKGROUND AND RELATED WORK

Data privacy, data utility, and the complexity of data transformation are serious issues that the data holder must consider when datasets are released to utilize in the outside scope of data-collecting organizations. For these reasons, several privacy preservation models have been proposed. Aside from privacy preservation models, we can also see data distortion techniques and data transformation algorithms are rapidly presented.

### 2.1 Privacy Preservation Model

Generally, privacy preservation models are the data framework such that they are used to address privacy violation issues when datasets are released to utilize in the outside scope of data-collecting organizations.

One of the most well-known privacy preservation models is  $k$ -anonymity [2]. It is a simple privacy preservation model. Moreover, it is widely applied in several real-life systems. For privacy preservation, all explicit identifier values of users are removed. Furthermore, the unique quasi-identifier values are distorted by their less specific values to be at least  $k$  indistinguishable tuples. Therefore, after datasets satisfy  $k$ -anonymity constraints, they can guarantee that all possible query conditions through the quasi-identifier attributes always have at least  $k$  tuples that are satisfied. However, in [3], the authors demonstrate that only removing the explicit identifier values and distorting the unique quasi-identifier values are not enough to address privacy violation issues in datasets because the sensitive data of users in datasets can still be violated by using identity and attribute linkage attacks.

To rid these vulnerabilities of  $k$ -anonymity, an extended  $k$ -anonymity model,  $l$ -diversity [3], is pro-

posed. With  $l$ -diversity, aside from removing the explicit identifier values and distorting the unique quasi-identifier values, the number of distinct sensitive values is further considered in privacy preservation constraints such that every group of indistinguishable quasi-identifier values must relate to at least  $l$  different sensitive values. Therefore, after datasets are satisfied by  $l$ -diversity constraints, they can guarantee that all possible query conditions through the quasi-identifier attributes always have at least  $l$  distinct sensitive values that are satisfied.

Unfortunately, the datasets satisfy  $l$ -diversity constraints. They still have concerns about privacy violation issues from considering the distance of sensitive values. To rid this vulnerability of  $l$ -diversity,  $t$ -closeness [4] is proposed. With  $t$ -closeness, the parameter  $t$  enables one to trade-off between data utility and data privacy in datasets. We limit the gain from  $dis_1$  to  $dis_2$  by the limitations of the distance between both values as  $v_1$  and  $v_2$ . Intuitively, if  $dis_1$  equals  $dis_2$ ,  $v_1$  and  $v_2$  are the same. If  $dis_1$  and  $dis_2$  are close,  $v_1$  and  $v_2$  are close. Also, when  $dis_1$  and  $dis_2$  are more different, it means that  $v_1$  and  $v_2$  are very different. For privacy preservation, the unique quasi-identifier values are distorted to be indistinguishable such that every group of distorted quasi-identifier values must relate to the set of the protected sensitive values that have the distance to be at least  $t$ . Therefore, after datasets satisfy  $t$ -closeness constraints, they can guarantee that the distance of re-identifying the protected sensitive values is at least  $t$ . Although datasets satisfy  $t$ -closeness constraints to be more secure in terms of privacy preservation than  $k$ -anonymity and  $l$ -diversity, they have data utility issues that must be addressed.

To address the data utility issues in high-dimension datasets,  $k^m$ -anonymity [5] is proposed. This privacy preservation model assumes that the adversary has the limitation of the background knowledge about the target user, i.e., the adversary has the background knowledge about the target user to be at most  $m$  values. Thus, only the  $m$ -size of unique quasi-identifier values are distorted to be at least  $k$  indistinguishable tuples. For this reason, after the datasets are satisfied by  $k^m$ -anonymity constraints, they can guarantee that every possible query condition through the  $m$ -size quasi-identifier attributes always has at least  $k$  tuples that are satisfied.

$LKC$ -privacy [6] is a privacy preservation model. It is also proposed to address privacy violation issues in high-dimension datasets. For privacy preservation, all at most  $L$  sizes of the unique quasi-identifier values are distorted to be at least  $K$  indistinguishable tuples. Moreover, every protected sensitive value in every group of the distorted quasi-identifier values must have the confidence of data re-identification to be at most  $C$ .

Aside from the mentioned-above privacy preserva-

tion models, other well-known models are also proposed to address privacy violation issues in released datasets such as  $(k, e)$ -anonymous [7] and  $(\alpha, k)$ -anonymity [8].

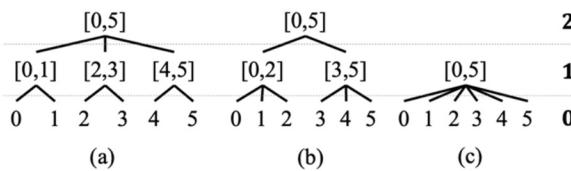
In [7],  $(k, e)$ -anonymous is proposed. For privacy preservation, before datasets are released, the tuples are firstly re-sorted by the sensitive values ascending. Then, the tuples are partitioned. That is, every partition must include at least  $k$  tuples. Moreover, every partition collects the sensitive values that have a different range between the lower and upper bounds to be at least  $e$ . Finally, the quasi-identifier tuples or the sensitive values of each partition are shuffled. For this reason, after datasets are satisfied by  $(k, e)$ -anonymous constraints, they can guarantee that the sensitive values have the confidence of the data re-identification to be at most  $e$ . Moreover, they can further guarantee that all possible queried results always have at least  $k$  tuples that are satisfied.

With  $(\alpha, k)$ -anonymity [8], it is proposed to address privacy violation issues by using probability inference linkage attacks. With this privacy preservation model,  $\alpha$  and  $k$  are both privacy preservation constraints. That is, before datasets are released, the unique quasi-identifier values are distorted to be at least  $k$  indistinguishable tuples. Moreover, every sensitive value must have the confidence of data re-identification from using probability inference linkage attacks to be at most  $\alpha$ . Therefore, after datasets satisfy  $(\alpha, k)$ -anonymity constraints, they can guarantee that the sensitive values cannot have any concern of privacy violation issues from using probability inference linkage attacks. Moreover, they can also guarantee that all possible queried results always have at least  $k$  tuples that are satisfied.

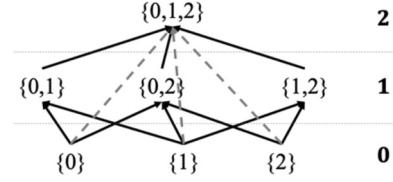
In brief, the privacy preservation model is the data model that is used to address privacy violation issues in datasets when they are released to the outside scope of data-collecting organizations.

## 2.2 Data Distortion

The data distortion technique is a data structure for distorting the unique values in released datasets to satisfy privacy preservation constraints. A few examples of well-known data distortion techniques are as follows.



**Fig.1:** A DGH of the rating scores as [0, 5].



**Fig.2:** A NDGH of the rating scores as [0, 2].

Domain Generalization Hierarchies (DGH) [2] is a well-known data structure that is proposed to describe the level of specificity quasi-identifier values that are available in datasets. They are based on tree data structures such that the values of the low level are more specific than the values that are available at the high level. Three examples are shown in Figure 3. They are proposed to present the level of data specifications for rating scores as [0, 5].

Natural Domain Generalization Hierarchies (NDGH) [10] is also a well-known data structure that is proposed to describe the level of specificity quasi-identifier values that are available in datasets. With NDGH, it is based on directed graphs such that the label of each node presents a set of quasi-identifier values. Moreover, the label values of the low level are more specific than the label values of the high level. An example of NDGH is shown in Figure 2. It is proposed to present the level of data specifications for rating scores as [0, 2].

Data swapping [7] is a data distortion technique that is widely acknowledged to apply in privacy preservation models. With this data distortion, the unique values in datasets are distorted by swapping their positions.

The range of data [10] is a data distortion technique that is often used to distort the unique numerical in datasets. That is, the uniquely numerical values do not have any concern of privacy violation issues when they are distorted by their range between the lower and upper bounds to be indistinguishable.

Another data distortion technique is often available in privacy preservation models. It is additive noises [11]. That is, the unique data is distorted by using some appropriate noises.

In brief, the data distortion technique is the data structure that is proposed to describe the level of the specificity values that are available in datasets.

## 2.3 Data Transformation

The data transformation is an algorithm. It is used for transforming datasets to satisfy privacy preservation constraints such as brute force [12] and clustering [13]. With brute force algorithms, they are a simple and classical idea for transforming datasets to satisfy privacy preservation constraints. Generally, they can guarantee that the released data version of datasets is optimal. However, they are highly complex. Thus,

they are unsuitable for addressing privacy violation issues in larger-size or high-dimension datasets. To rid this vulnerability of brute force algorithms, the privacy preservation models are based on clustering algorithms to be proposed. That is, before datasets are released to utilize in the outside scope of data-collecting organizations, the similar tuples are firstly clustered to be the groups. Finally, the unique values of each group are distorted by their less specific values to be indistinguishable. The most well-known privacy preservation model,  $k$ -member [13], is based on clustering algorithms in conjunction with  $k$ -anonymity constraints. For privacy preservation, the at least  $k$  size of tuple groups is constructed by considering their distance scores. Another well-known privacy preservation model is based on clustering algorithms. It is Mondrian Multidimensional  $k$ -anonymity [14]. With this privacy preservation model, the most similarity of tuples in each group is constructed by a strict multi-dimensional partitioning algorithm. However, we can see that these privacy preservation models still are complex. To rid this vulnerability, a privacy preservation technique is based on the weighted graph of correlated generalization tuples and the adjacency matrix of tuple distances to be proposed in this work.

In brief, data transformations are algorithms that can transform datasets to satisfy privacy preservation constraints. A desired data transformation algorithm is low complexity and can maintain the data utility of datasets as much as possible.

### 3. THE PROPOSED MODEL

In this section, we propose both privacy preservation models. They are based on  $k$ -anonymity in conjunction with a weighted graph of correlated generalization tuples and an adjacency matrix of tuple distances. Before the proposed technique will be presented. We first define the necessary basic definitions of this work.

**Definition 1 (Dataset)** Let  $U = \{u_1, u_2, \dots, u_n\}$  be the set of users. Let  $D = \{d_1, d_2, \dots, d_n\}$  be the original dataset that is constructed from  $n$  user tuples such that every  $d_i \in D$  represents the profile tuple of the user  $u_i \in U$ , where  $1 \leq i \leq n$ . Moreover, every  $d_i$  constructs from  $m$  attributes as  $A = \{a_1, a_2, \dots, a_m\}$ . That is,  $QI = \{qi_1, qi_2, \dots, qi_{m-1}\} \subset A$  is the set of quasi-identifier attributes. Another attribute  $S \in A$  (i.e.,  $A - QI$ ) is the sensitive attribute. In addition, let  $D[qi_y]$ , where  $1 \leq y \leq |QI|$ , be the data projection of  $qi_y$  of  $D$ . Let  $D[S]$  be the data projection of  $S$  of  $D$ . Let  $D[QI]$  be the data projection of all quasi-identifier tuples that are available in  $D$ . Let  $d_i[QI]$  be the data projection of the quasi-identifier tuple of  $d_i$ . Moreover, let  $d_i[S]$  be the data projection of the sensitive value of  $d_i$ .

For example, let Table 1 be the original dataset  $D$  that has seven user profile tuples (i.e.,  $d_1, d_2, d_3, d_4, d_5, d_6$ , and  $d_7$ ) and three attributes, i.e.,

**Table 3:** The data projection of  $D[d_1]$  of Table 1.

#ID	Age	Gender	Disease
$d_1$	45	Male	Flu

Age, Gender, and Disease. Let Age and Gender be the quasi-identifier attributes. The Disease is a sensitive attribute. Therefore, the  $D[d_1]$  of Table 1 is shown in Table 3. The  $D[S]$  of Table 1 is shown in Table 4. The  $D[QI]$  of Table 1 is shown in Table 5. The  $d_1[QI]$  of Table 1 is shown in Table 6. The  $d_1[S]$  of Table 1 is shown in Table 7.

**Table 4:** The data projection of  $D[S]$  of Table 1.

#ID	Disease
$d_1$	Flu
$d_2$	Fever
$d_3$	Cancer
$d_4$	HIV
$d_5$	Flu
$d_6$	HIV
$d_7$	Fever

**Table 5:** The data projection of  $D[QI]$  of Table 1.

#ID	Age	Gender
$d_1$	45	Male
$d_2$	46	Female
$d_3$	47	Male
$d_4$	48	Male
$d_5$	48	Female
$d_6$	42	Female
$d_7$	42	Female

**Table 6:** The data projection of  $d_1[QI]$  of Table 1.

#ID	Age	Gender
$d_1$	45	Male

**Table 7:** The data projection of  $d_1[S]$  of Table 1.

#ID	Disease
$d_1$	Flu

**Definition 2 (Privacy Violation Issues)** Let  $D$  be the specified dataset. Let  $k$  be the minimum number of tuples that cannot have any concerns about privacy violation issues. The meaning of privacy violation issues for a tuple  $d_i \in D$  is that  $d_i[QI]$  is duplicated by other quasi-identifier tuples in  $D[QI]$  to be at most  $k - 1$  tuples.

In addition, the data domain of  $qi_y \in QI$  is generally numerical and non-numerical. The numerical data is the data that can be quantifiable, e.g., age and salary. With the non-numerical data, it is categorical data such as gender, position, and education.

For this reason, they can be distorted to satisfy privacy preservation constraints through a different data transformation technique.

### 3.1 Data Distortion Based on Numerical Data

Let  $qi_y \in QI$  be a specified quasi-identifier attribute of  $D$  such that the data domain of  $qi_y$  is numerical. Given  $\vartheta \subseteq qi_y$  is the set of the particular quasi-identifier values from  $qi_y$ . With  $\vartheta$ , it can be distorted to be indistinguishable from using their range between  $f_{MIN}(\vartheta)$  and  $f_{MAX}(\vartheta)$ . More range between  $f_{MIN}(\vartheta)$  and  $f_{MAX}(\vartheta)$  is more secure in terms of privacy preservation. Therefore, the distorted value distance of  $\vartheta$  can be defined by  $f_{dis}(\vartheta) : f_{MAX}(\vartheta) - f_{MIN}(\vartheta)$ .

For example, let the Age attribute of Table 1 be the specified quasi-identifier attribute. Let 45, 46, and 48 be the particular quasi-identifier values.  $f_{MIN}(\{45, 46, 48\})$  is 45.  $f_{MAX}(\{45, 46, 48\})$  is 48. Therefore, the distorted value of them is “45-48”. The distorted value distance of them is 3, i.e.,  $48-45=3$ .

### 3.2 Data Distortion Based on Non-Numerical Data

This section is proposed to explain the technique that can be used for distorting non-numerical quasi-identifier values to be indistinguishable. Let  $qi_y \in QI$  be a quasi-identifier attribute. Let  $DO^{qi_y} = \{do_1^{qi_y}, do_2^{qi_y}, \dots, do_z^{qi_y}\}$  be the data domain of  $qi_y$ . Let  $f_{DGH}(DO_L^{qi_y}) : DO_L^{qi_y} \rightarrow DO_{L+1}^{qi_y}$  be the distortion function of  $DO^{qi_y}$  from the level  $L$  to the level  $L + 1$  such that all values of the level  $L$  are more specific than all values that are available in the level  $L + 1$ . From the function, the domain distortion hierarchy of  $qi_y$ ,  $DGH_{qi_y}$ , can be defined

from a distortion sequence as  $DO_0^{qi_y} \xrightarrow{f_{DGH}(DO_0^{qi_y})} DO_1^{qi_y} \xrightarrow{f_{DGH}(DO_1^{qi_y})} DO_2^{qi_y} \dots DO_{L-2}^{qi_y} \xrightarrow{f_{DGH}(DO_{L-2}^{qi_y})} DO_{L-1}^{qi_y} \xrightarrow{f_{DGH}(DO_{L-1}^{qi_y})} DO_L^{qi_y}$ , where  $DO_0^{qi_y} = DO^{qi_y}$ . That is, the most specific values are available in the level 0 and the lowest specific values are available in the level L. Let  $\vartheta \subseteq qi_y$  be the set of the particular quasi-identifier values in  $qi_y$ . Let  $\omega$  be the distorted value of  $\vartheta$  such that  $\omega$  is available in the level  $\Phi$  of  $DGH_{qi_y}$ . Thus, the distorted value distance of  $\vartheta$  is  $\Phi$ , i.e.,  $f_{dis}(\vartheta) : \Phi$ .

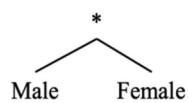


Fig.3:  $DGH_{Gender}$ .

For example, let the Gender attribute of Table 1 be the specified quasi-identifier attribute. Let Figure

3 be  $DGH_{Gender}$ . Moreover, suppose that the gender value is available in  $d_1$  and  $d_2$  to be the particular quasi-identifier values. Thus, the appropriately distorted value of the particular quasi-identifier values is \*. The distorted value distance of the particular quasi-identifier values is 1 because \* is available in the level 1 of  $DGH_{Gender}$ .

### 3.3 The Distance of Tuples

Let  $D_{SEL} \subseteq D$  be the set of the specified tuples. Let  $f_{dis}(D_{SEL}[qi_1]), f_{dis}(D_{SEL}[qi_2]), \dots, f_{dis}(D_{SEL}[qi_{m-1}])$  be the functions that represent the distorted value distance of  $D_{SEL}[qi_1], D_{SEL}[qi_2], \dots, D_{SEL}[qi_{m-1}]$ , respectively. Therefore, the distorted value distance of  $D_{SEL}$  can be defined by  $f_{DIS}(D_{SEL}) : f_{dis}(D_{SEL}[qi_1]) + f_{dis}(D_{SEL}[qi_2]) + \dots + f_{dis}(D_{SEL}[qi_{m-1}])$ . More value of  $f_{DIS}(D_{SEL})$  is more secure in terms of privacy preservation.

For example, let Table 1 be the original dataset  $D$ . Let  $d_1$  and  $d_2$  be both of the particular tuples in Table 1, i.e.,  $D_{SEL} = \{d_1, d_2\}$ . Let Figure 3 be  $DGH_{Gender}$ . In this situation, a distorted data version of Table 1 is shown in Table 8. That is, the Age attribute,  $D_{SEL}[Age]$ , is distorted by the range of users' ages that are available in the Age attribute of  $d_1$  and  $d_2$ , i.e., 45 - 46. Moreover, the unique gender values in the Gender attribute,  $D_{SEL}[Gender]$ , are distorted by an appropriate value, \*, that is available in  $DGH_{Gender}$ . Therefore, Table 8 has the distorted value distance to be 2, i.e.,  $1 + 1 = 2$ .

Table 8: A distorted data version of  $d_1$  and  $d_2$  of Table.

#ID	Age	Gender	Disease
$d_1$	45 - 46	*	Flu
$d_2$	45 - 46	*	Fever

### 3.4 Privacy preservation is Based on k-anonymity in conjunction with Weighted Graphs and Adjacency Matrix

This section is devoted to presenting both privacy preservation models. They are based on the weighted graph of correlated distortion tuples and the adjacency matrix of tuple distances to be proposed. The proposed technique aims to transform datasets to satisfy  $k$ -anonymity constraints.

**Definition 3 (The Weighted Graph of Correlated Distortion Tuples)** Let  $G = (V, E)$  be a weighted graph that proposes to present the correlated distortion tuples of  $D$ . That is,  $V$  is the set of vertices such that every  $v_i \in V$  represents the tuple  $d_i$  of  $D$ , while  $E = \{v_\alpha, v_\beta\} | v_\alpha, v_\beta \in V \text{ and } v_\alpha \neq v_\beta\}$  is the set of edges that represent the relationship between the vertices  $v_\alpha$  and  $v_\beta$ . Moreover, each edge of  $v_\alpha$  and  $v_\beta$  has an associated numerical value (a weight) that represents  $f_{dis}(v_\alpha, v_\beta)$ .

**Definition 4 (The Adjacency Matrix of Distorted Tuple Distances)** Let  $G = (V, E)$  be a weighted graph of correlated distortion tuples. An adjacency matrix of  $G = (V, E)$  is  $GM = [gm_\alpha, gm_\beta]_{n \times n}$ , where  $0 \leq \alpha \leq n$  and  $0 \leq \beta \leq n$ , such that  $GM = [gm_\alpha, gm_\beta]_{n \times n}$  is in the form of  $\begin{bmatrix} 0 & \Delta GM^T \\ \Delta GM & 0 \end{bmatrix}$ , i.e., the  $(gm_\alpha, gm_\beta)$ -position of  $GM$  collects  $f_{dis}(gm_\alpha, gm_\beta)$ , otherwise, it collects 0. Therefore,

$$GM[gm_\alpha, gm_\beta] = \begin{bmatrix} gm_0, gm_\beta \\ gm_1, gm_\beta \\ \vdots \\ gm_n, gm_\beta \end{bmatrix}$$

Is equal to

$$GM[gm_\beta, gm_\alpha]^T = [gm_\beta, gm_0 \ gm_\beta, gm_1 \ \dots \ gm_\beta, gm_n].$$

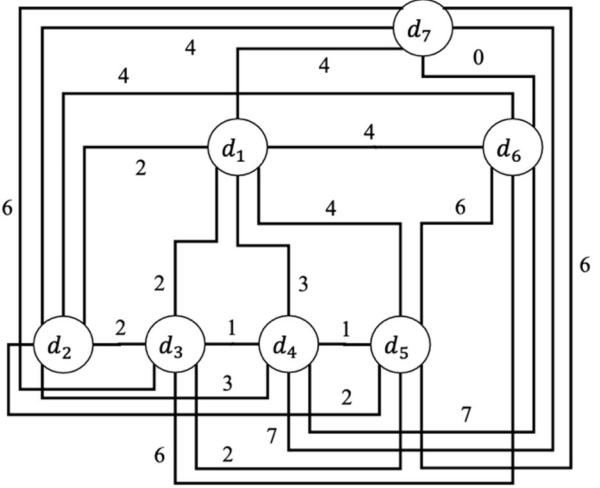
**Definition 5 (Equivalence Class)** Let a positive integer  $k$ , where  $k \in I^+$  and  $k \geq 2$ , be the privacy preservation constraint. Let  $D_{SEL} \subseteq D$  be the set of the specified tuples such that the size of  $D_{SEL}$  is at least  $k$ , i.e.,  $|D_{SEL}| \geq k$ . Let  $ec$  be an equivalence class that can be constructed from  $D_{SEL}$  by using  $f_A(D_{SEL}) : D_{SEL} \rightarrow D'_{SEL}$ , i.e.,  $ec = D'_{SEL}$ . That is, the unique quasi-identifier values of  $D'_{SEL}$  are distorted by their less specific values that are presented in the form of the  $DGH$  or the value range of them.

**Definition 6 (The Error of Equivalence Classes)** Let  $ec$  be an equivalence class that is constructed from  $D_{SEL} \subseteq D$ . Thus, the error of  $ec$  can be defined by  $f_{err}(ec) : f_{DIS}(D_{SEL}) * |D_{SEL}|$ .

### 3.4.1 Privacy Preservation Based on The Adjacency Matrix of Distorted Tuple Distances

Let  $D = \{d_1, d_2, \dots, d_n\}$  be the original dataset. Let  $G = (V, E)$  be a weighted graph of correlated distortion tuples of  $D$ . Let  $GM$  be an adjacency matrix of  $G = (V, E)$ . With  $GM$ , we know that it is a symmetric matrix, i.e.,  $GM[gm_\alpha, gm_\beta] = GM[gm_\beta, gm_\alpha]^T$ . Thus, only the lower or upper triangular matrix of the adjacency matrix of  $GM$  is considered for constructing the desired released dataset  $D'$  of  $D$ , i.e.,  $\Delta GM$ . Let  $f_A(D, \Delta GM, k) : D \rightarrow_{\Delta GM, k} D'$  be the function for transforming  $D$  to become  $D'$ . That is, the users' unique quasi-identifier values in  $D'$  are distorted to be at least  $k$  indistinguishable quasi-identifier tuples by using their ranges between the lower and upper bounds or the less specific values that are available in the  $DGH$  of them. Moreover, the summation of every group of indistinguishable quasi-identifier tuples in  $\Delta GM$  must be minimized. In addition, aside from the list of tuples,  $D'$  further has another view that is

in the form of the set of its equivalence classes, i.e.,  $EC = \{ec_1, ec_2, \dots, ec_e\}$ . Without loss of generality, every equivalence class  $ec_p$ , where  $1 \leq p \leq e$ , of  $D'$  must satisfy the data limitations that are  $\bigcup_{p=1}^e ec_p = D$  and  $\bigcap_{p=1}^e ec_p = \emptyset$ .



**Fig.4:** A weighted graph of the correlated distortion tuples.

For example, let Table 1 be the original dataset  $D$ . Moreover, the  $DGH$  of the Gender attribute is shown in Figure 3. A correlated distortion tuple graph of Table 1 is shown in Figure 4. Thus, the adjacency matrix of Table 1 is shown in Figure 5. While the lower triangular matrix of the adjacency matrix is shown in Figure 6 and the upper triangular matrix of the adjacency matrix is shown in Figure 7. In addition, in this example, only the lower triangular matrix of the adjacency matrix is used to consider constructing the appropriate released data version of Table 1. Suppose the value of  $k$  is 2. A released data version of Table 1 is shown in Table 9. Table 9 has three equivalence classes. The first equivalence class constructs from  $d_6$  and  $d_7$ . The cause of  $d_6$  and  $d_7$  is available in the first equivalence class, it is that the distance between  $d_6$  and  $d_7$  is closer than other tuples, i.e., the distance between  $d_6$  and  $d_7$  is 0 (zero). In addition, after the first equivalence class is constructed successfully,  $d_6$  and  $d_7$  will not be considered. Currently, Table 1 only remains five tuples, i.e.,  $d_1, d_2, d_3, d_4$ , and  $d_5$ . With the remaining tuples, we can see that  $(d_3, d_4)$ -position and  $(d_3, d_5)$ -position collect the same tuple distance and they are closest than other remaining tuples, i.e., they have the tuple distance to be 1. Moreover,  $(d_3, d_4)$ -position and  $(d_4, d_5)$ -position are associated through  $d_4$ , so,  $d_3, d_4$ , and  $d_5$  are constructed to be the second equivalence class of the released dataset. In this situation, only  $d_1$  and  $d_2$  are not investigated. Moreover, they are fit for only constructing an equivalence class. Thus, the third equivalence class is constructed from two remaining tuples as  $d_1$  and  $d_2$ . For this reason, the error

of Table 9 is 10, i.e.,  $((1+1)*2)+((1+1)*3)=4+6=10$ .

	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$	$d_7$
$d_1$	0	2	2	3	4	4	4
$d_2$	2	0	2	3	2	4	4
$d_3$	2	2	0	1	2	6	6
$d_4$	3	3	1	0	1	7	7
$d_5$	4	2	2	1	0	6	6
$d_6$	4	4	6	7	6	0	0
$d_7$	4	4	6	7	6	0	0

**Fig.5:** An adjacency matrix of Table1.

	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$	$d_7$
$d_1$	0						
$d_2$	2	0					
$d_3$	2	2	0				
$d_4$	3	3	1	0			
$d_5$	4	2	2	1	0		
$d_6$	4	4	6	7	6	0	
$d_7$	4	4	6	7	6	0	0

**Fig.6:** A lower triangular matrix of the adjacency matrix of Table 1.

	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$	$d_7$
$d_1$	0	2	2	3	4	4	4
$d_2$	0	2	3	2	4	4	
$d_3$	0	1	2	6	6		
$d_4$	0	1	7	7			
$d_5$	0	6	6				
$d_6$	0	0					
$d_7$	0						

**Fig.7:** A upper triangular matrix of the adjacency matrix of Table 1.

**Table 9:** A distorted data version of Table 1 satisfies  $k = 2$  by using the proposed data transformation technique.

#ID	Age	Gender	Disease
$d_6$	42	Female	HIV
$d_7$	42	Female	Fever
$d_3$	47 - 48	*	Cancer
$d_4$	47 - 48	*	HIV
$d_5$	47 - 48	*	Flu
$d_1$	45 - 46	*	Flu
$d_2$	45 - 46	*	Fever

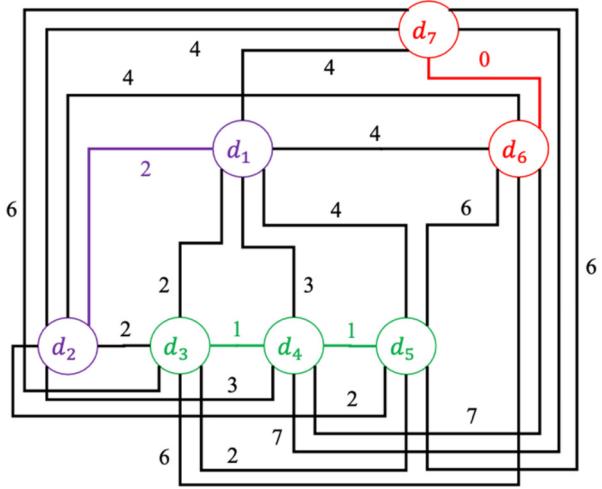
Another example of privacy preservation is based on  $k$ -anonymity constraints in conjunction with the adjacency matrix of distorted tuple distances. Also, let Table 1 be the original dataset  $D$  and let Figure 3 be  $DGH_{Gender}$ . Let the value of  $k$  be 3. In this situation, the first equivalence class of the released dataset of Table 1 is constructed from the tuples  $d_3$ ,  $d_4$ , and  $d_5$  because the tuple distance of them is only 3, i.e.,  $2 + 1 = 3$ . Another equivalence class of the dataset is constructed from the tuples  $d_1$ ,  $d_2$ ,  $d_6$ , and

$d_7$ . Therefore, Table 10 is a released data version of Table 1 such that it satisfies 3-anonymity constraints. With this released data version of Table 1, it has the error to be 26, i.e.,  $((1+1)*3)+((4+1)*4)=6+20=26$ .

**Table 10:** A distorted data version of Table 1 satisfies  $k = 2$  by using the proposed data transformation technique.

#ID	Age	Gender	Disease
$d_3$	47 - 48	*	Cancer
$d_4$	47 - 48	*	HIV
$d_5$	47 - 48	*	Flu
$d_1$	42 - 46	*	Flu
$d_2$	42 - 46	*	Fever
$d_6$	42 - 46	*	HIV
$d_7$	42 - 46	*	Fever

Aside from the adjacency matrix of distorted tuple distances, the distorted data versions of  $D$  can also be constructed from the weighted graph of correlated distortion tuples of  $D$  directly.



**Fig.8:** A graphic info for demonstrating the relationship of the similar tuples for constructing the suitable equivalence classes of Table 1, where  $k = 2$ .

**Table 11:** A partitioned data version of Table 1.

#ID	Age	Gender	Disease
$d_6$	42	Female	HIV
$d_7$	42	Female	Fever
$d_3$	47	Male	Cancer
$d_4$	48	Male	HIV
$d_5$	48	Female	Flu
$d_1$	45	Male	Flu
$d_2$	46	Female	Fever

### 3.4.2 Privacy Preservation Based on The Weighted Graph of Correlated Distortion Tuples

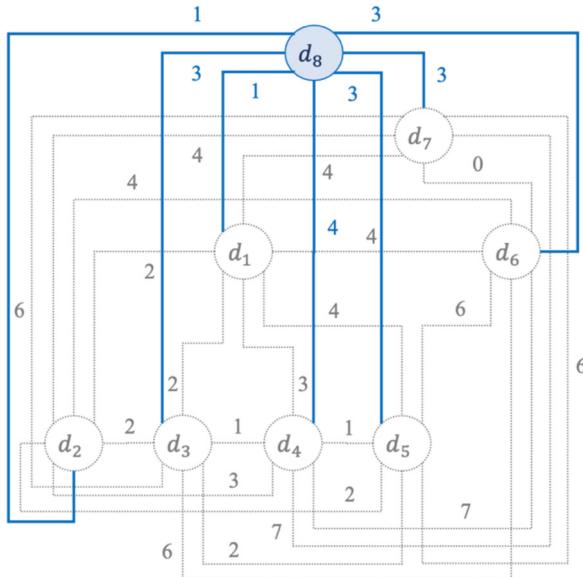
Let  $G = (V, E)$  be a weighted graph of correlated distortion tuples of  $D$ . Let  $G_{SUB} = \{G_1, G_2, \dots, G_q\}$  be the set of disjoint sub-graphs of  $G$ . Let  $E_r = \{\{v_\alpha, v_\beta\} | v_\alpha, v_\beta \in G_r \text{ and } v_\alpha \neq v_\beta\}$  be the set of edges in  $G_r$ , where  $1 \leq r \leq q$ . For privacy preservation,  $G_{SUB}$  is first satisfied the limitations as follows,

- $G_1 \cup G_2 \cup \dots \cup G_q = V$
- $G_1 \cap G_2 \cap \dots \cap G_q = \emptyset$
- $|G_r| \geq k$ , where  $1 \leq r \leq q$ , and
- the summation of the weighted edges of  $G_1, G_2, \dots, G_q$  is minimized.

Then, the tuples of  $D$  are partitioned to correspond  $G_{SUB}$ . Finally, all users' unique quasi-identifier values in each partition are distorted by using their ranges between the lower and upper bounds or a less specific value that is available in the  $DGH$  of them.

**Table 12:** The data version of Table 1 is after inserted  $d_8$ .

#ID	Age	Gender	Disease
$d_1$	45	Male	Flu
$d_2$	46	Female	Fever
$d_3$	47	Male	Cancer
$d_4$	48	Male	HIV
$d_5$	48	Female	Flu
$d_6$	42	Female	HIV
$d_7$	42	Female	Fever
$d_8$	45	Female	Cancer



**Fig.9:** The weighted graph of correlated generalization tuples after inserts  $d_8$ .

For example, let Table 1 be the original dataset  $D$ . Let the value of  $k$  be 2. Let Figure 4 be the

weighted graph of correlated distortion tuples of Table 1. Therefore, an appropriate  $G_{SUB}$  version of Figure 4 such that it is satisfied by  $k = 2$  to be shown in Figure 8. That is, the weighted graph of correlated distortion tuples of Table 1 can be separated to be three appropriate sub-graph versions. The first sub-graph version includes both vertices as  $d_6$  and  $d_7$  (the red vertices). While three vertices construct the second sub-graph version as  $d_3$ ,  $d_4$ , and  $d_5$  (the green vertices). Another appropriate sub-graph version consists of  $d_1$  and  $d_2$  (the purple vertices). Thus, the partitioned data version of Table 1 is accorded to the sub-graph of its weighted graph to be shown in Table 11. After that, the unique values are available in each quasi-identifier of every partition to be distorted by their less specific values, i.e., the unique users' ages of each partition are distorted by their range, and the unique users' genders are distorted by an appropriately less specific value of them such that it is available in its  $DGH$  as shown in Figure 3. Therefore, a released data version of Table 1 is Table 9.

	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$	$d_7$	$d_8$
$d_1$	0	2	2	3	4	4	4	1
$d_2$	2	0	2	3	2	4	4	1
$d_3$	2	2	0	1	2	6	6	3
$d_4$	3	3	1	0	1	7	7	4
$d_5$	4	2	2	1	0	6	6	3
$d_6$	4	4	6	7	6	0	0	3
$d_7$	4	4	6	7	6	0	0	3
$d_8$	1	1	3	4	3	3	3	0

**Fig.10:** The adjacency matrix of Table 12 is after  $d_8$  to be inserted.

In addition, the examples are discussed in Sections 3.4.1 and 3.4.2. We can see that the weighted graph of correlated distortion tuples and the adjacency matrix of Table 1 do not have any data changes. For this reason, we can conclude that if the data of  $D$  is not changed, only the first time has the cost for building the weighted graph of correlated distortion tuples and the adjacency matrix of  $D$ . Although the data of  $D$  is changed, the cost of building the weighted graph of correlated distortion tuples and the adjacency matrix of  $D$  only has the effect of the number of tuple changes.

For example, suppose that the new tuple  $d_8$  is inserted into Table 1 such that it is shown in Table 12. Thus, the weighted graph of correlated distortion tuples and the adjacency matrix are shown in Figures 9 and 10, respectively. In this example, it is clear that when the data of  $D$  is changed when the new data becomes available, only the related new data are changed in the weighted graph of correlated distortion tuples and the adjacency matrix of  $D$ .

## 4. DATA UTILITY METRIC

Although  $D'$  is generally higher security in terms of privacy preservation than its original  $D$ . We can see that  $D'$  loses some data utility. For this reason, only  $D'$  is highly data utilities to be desired. Thus, the data utility metric is a necessity. Since privacy preservation based on  $k$ -anonymity constraints has been presented, several data utility metrics are proposed, e.g., Precision metric (PREC) [2], Discernibility metric (DM) [15], and Relative error [7].

### 4.1 Precision Metric (PREC) [2]

With the proposed models,  $D'$  is based on data distortions. For this reason, the penalty cost of  $D'$  depends on the distance and the number of distorted values. For the non-numerical quasi-identifier values, the penalty cost of data distortion for  $D'$  can be defined by Equation 1.

$$f_{D_1}(d_i, QI, DGH_{qi_y}) = \sum_{y=1}^{|QI|} \frac{f_{dis}(d_i[qi_y])}{|DGH_{qi_y}|}$$

$$f_{GEN1}(D', DGH_{qi_y}) = \frac{\sum_{i=1}^{|D'|} f_{D_1}(d_i, QI, DGH_{qi_y})}{|D'| * |QI|} \quad (1)$$

Where,

■  $|QI|$  is the number of quasi-identifier attributes that are available in  $D$ .

■  $f_{dis}(d_i[qi_y])$  is the distance of the distorted value that is available in  $qi_y$  of  $d_i$ .

■  $|DGH_{qi_y}|$  is the height of the  $DGH$  for  $DO^{qi_y}$

■  $|D'|$  is the number of tuples that are available in  $D$ .

For the numerical quasi-identifier values, the penalty cost of data distortion for  $D'$  can be defined by Equation 2.

$$f_{D_2}(d_i, QI, DGH_{qi_y}) = \sum_{y=1}^{|QI|} \frac{f_{dis}(d_i[qi_y])}{f_{MAX}(qi_y) - f_{MIN}(qi_y)}$$

$$f_{GEN2}(D', DGH_{qi_y}) = \frac{\sum_{i=1}^{|D'|} f_{D_2}(d_i, QI, DGH_{qi_y})}{|D'| * |QI|} \quad (2)$$

Where,

■  $f_{MAX}(qi_y)$  is the maximum value that is available in  $qi_y$  of  $D$ .

■  $f_{MIN}(qi_y)$  is the minimum value that is available in  $qi_y$  of  $D$ .

### 4.2 Discernibility Metric (DM) [15]

The DM metric is a data utility metric that can also be used to define the penalty cost or the data utility of  $D'$ . With the DM metric, the penalty cost of  $D'$  depends on the size of equivalence classes. The

larger size of equivalence classes leads to more penalty cost DM. Therefore, the DM penalty cost of  $D'$  can be defined by Equation 3.

$$f_{DM}(D') = \sum_{p=1}^{|EC|} |ec_p|^2 \quad (3)$$

Where,

■  $|EC|$  is the number of equivalence classes that are available in  $D'$ .

### 4.3 Relative Error [7]

The relative error is a metric that can also define the penalty cost of  $D'$ . With this metric, the data utility of  $D'$  depends on the difference in the query results between  $D'$  and  $D$ . The more relative error means that  $D'$  has less data utility. For query results that are numerical data, their relative errors can be defined by Equation 4.

$$f_{RE1}(v, v_0) = \frac{|v - v_0|}{v} \quad (4)$$

Where,

■  $v$  is the result that is queried from  $D$ .

■  $v_0$  is the relative result of  $v$  such that it is queried from  $D'$ .

With query results that are not numerical data, their relative errors can be defined by Equation 5.

$$f_{RE1}(n(v), n(v_0)) = \frac{|n(v) - n(v_0)|}{n(v)} \quad (5)$$

Where,

■  $n(v)$  is the number of values that are queried from  $D$ .

■  $n(v_0)$  is the number of the relative values of  $n(v)$  such that they are queried from  $D'$ .

## 5. EXPERIMENT

In this section, the effectiveness and efficiency of the proposed privacy preservation models are discussed by comparison with  $k$ -member [13] and Mondrian Multidimensional  $k$ -anonymity [14].

### 5.1 Experimental Setup

All experiments are proposed to evaluate the effectiveness and efficiency of the proposed privacy preservation model, they are conducted on both Intel(R) Xeon(R) Gold 5218 @2.30 GHz CPUs with 64 GB memory and six 900 GB HDDs with RAID-5. Furthermore, all implementations are built and executed on Microsoft Windows Server 2019 in conjunction with Microsoft Visual Studio 2019 Community Edition and Microsoft SQL Server 2019. Moreover, they are discussed and conducted on the Adult dataset which is available at the UCI Machine Learning Repository [16]. This dataset is constructed from 32561 user profile tuples. Each user profile tuple consists of 14 attributes, i.e., Age, Workclass, Fnlwgt,

Education, Education-num, Marital-status, Occupation, Relationship, Race, Sex, Capital-gain, Capital-loss, Hours-per-week, and Native-country. To conduct effective experiments, only the attributes Age, Education, Marital-status, Occupation, Sex, Capital-loss, and Native-country are available in the experimental dataset. The attributes Age, Education, Marital-status, Occupation, Sex, and Native-country are set to be the quasi-identifier attributes, and another attribute, Capital-loss, is set to be the sensitive attribute. Moreover, all user profile tuples include the values “?” and “0”, they are removed. Therefore, the experimental dataset only includes 1428 user profile tuples.

## 5.2 Experimental Results and Discussion

### 5.2.1 Effectiveness

In this section, the effectiveness of the proposed privacy preservation models is evaluated by the PREC, DM, and relative error metrics.

In the first experiment, we propose to evaluate the effect of the given value of  $k$  that influences the data utility of datasets. All experimental results are discussed. They are based on the PREC penalty cost. Moreover, all tuples and all attributes are available in the experiments, and the value of  $k$  is varied from 2 to 20.

From the experimental results shown in Figure 11, we can see that the value of  $k$  influences the data utility of datasets (i.e., the number and the level of distorted values in the datasets). That is, the value of  $k$  is when increased. The number and the level of distorted values in the datasets also increase. Because the value of  $k$  directly influences the size of equivalence classes and the level of distorting quasi-identifier values. Moreover, we can see that both of the proposed privacy preservation models are more effective than both of the compared privacy preservation models, and we can further see that  $k$ -member is more effective than Mondrian Multidimensional  $k$ -anonymity. That is because the equivalence classes of both proposed privacy preservations are built from more similarity tuples than the equivalence classes that are constructed by both of the compared privacy preservation models.

In the second experiment, we propose to evaluate the effect of the number of quasi-identifier attributes that influence the data utility of datasets. All experimental results are based on the PREC penalty cost. Moreover, all tuples are available in the experiments. The value of  $k$  is fixed to be 10. The number of quasi-identifier attributes is varied from 1 to 6.

From the experimental results shown in Figure 12, we can see that the number of quasi-identifier attributes also influences the number and the level of distorted values in the datasets. It is when the number of quasi-identifier attributes that are increased. The number and the level of distorted values in the

datasets also increase. However, the number of quasi-identifier attributes influences the level of distorted values in the equivalence classes to be less than the value of  $k$ . Also, both proposed privacy preservation models are more effective than the compared privacy preservation models in all experiments.

In the fourth experiment, we propose to evaluate the effect of the value of  $k$  that influences the size of equivalence classes in datasets. All experimental results are based on the DM penalty cost. Moreover, all tuples and all attributes are available in the experiments. The value of  $k$  is varied from 2 to 20.

From the experimental results shown in Figure 14, we can see that the value of  $k$  directly influences the DM penalty cost of datasets or the size of equivalence classes of datasets. The large size of equivalence classes leads to more DM penalty cost of datasets. Also, both proposed privacy preservation models are more effective than the compared privacy preservation models in all experimental results.

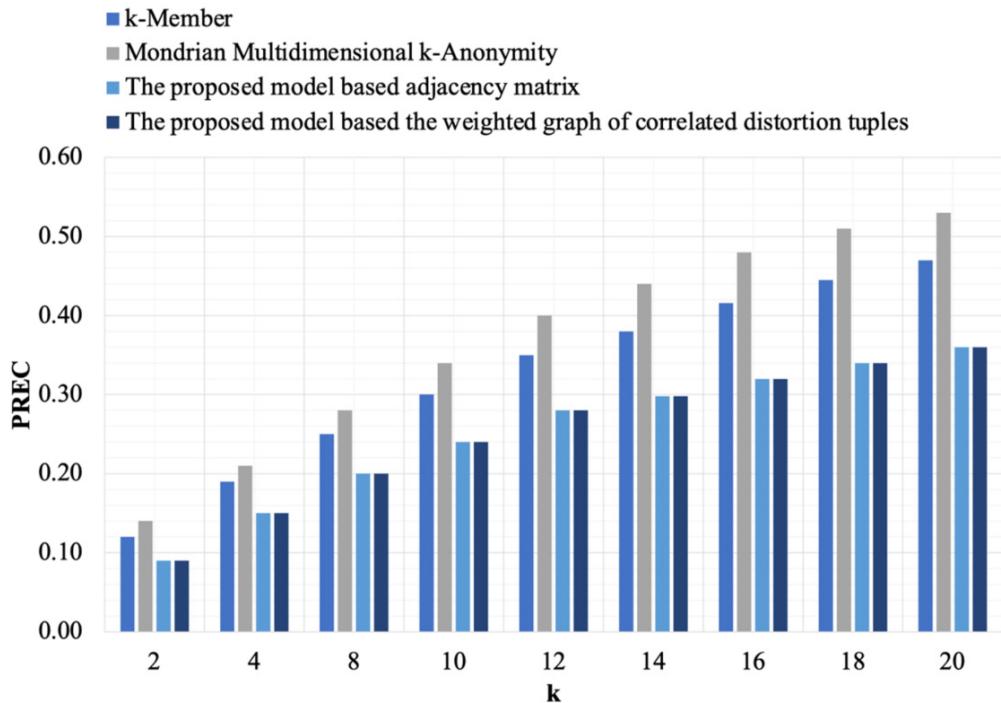
In the third experiment, we propose to evaluate the effect of the size of datasets that influences the data utility of datasets. All experimental results are also based on the PREC penalty cost. Moreover, all quasi-identifier attributes are available in the experiments. The value of  $k$  is fixed to be 10. The size of datasets is varied from 200 to 1400.

From the experimental results that are shown in Figure 13, we can see that when the size of datasets is increased, the number and the level of distorted values in the datasets is decreased, or we can say that when the size of datasets is increased, the data utility of datasets is also increased. That is because when the size of datasets is increased, the variety of values in the datasets is also increased. Also, both proposed privacy preservation models are more effective than the compared privacy preservation models in all experimental results of the third experiment.

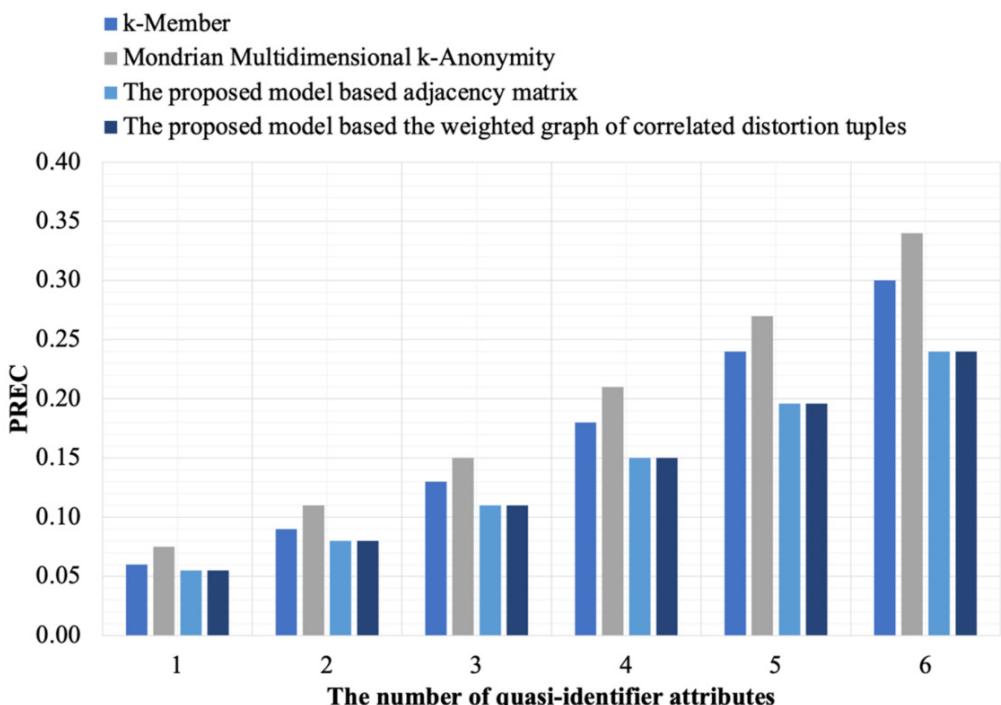
In the fifth experiment, we propose to evaluate the effect of the number of quasi-identifier attributes that influence the size of equivalence classes in datasets. All experimental results are based on the DM penalty cost. Moreover, all tuples are available in the experiments. The value of  $k$  is fixed to be 10. The number of quasi-identifier attributes is varied from 1 to 6.

From the experimental results shown in Figures 14 and 15, the number of quasi-identifier attributes also influences the size of equivalence classes. However, they are less effective than the value of  $k$ . Also, both proposed privacy preservation models are more effective than the compared privacy preservation in all experimental results.

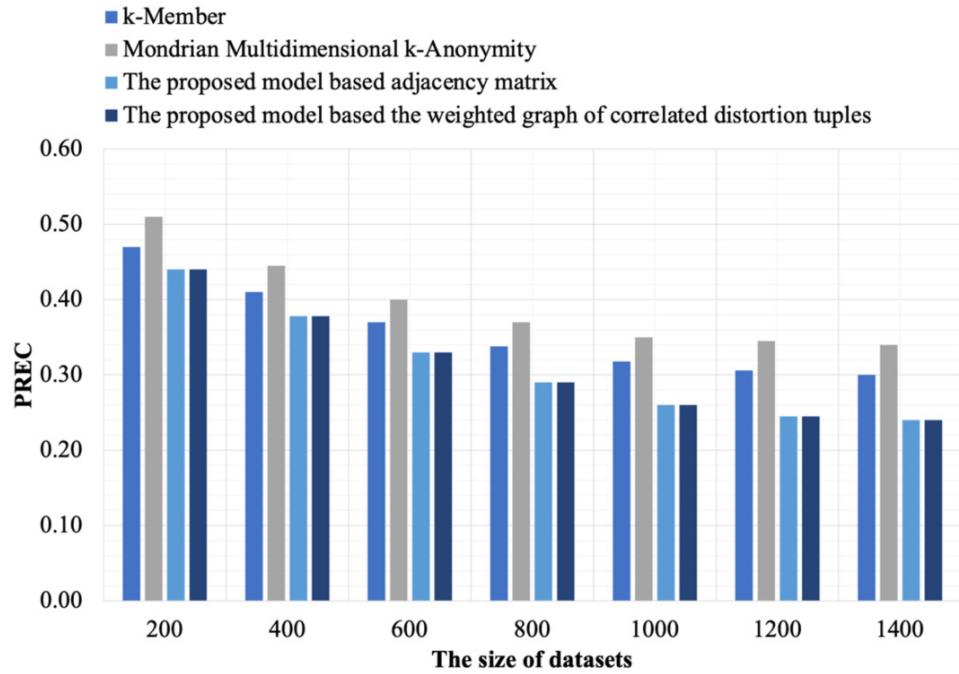
In the sixth experiment, we propose to evaluate the effect of the number of quasi-identifier attributes that influence the query results that are queried by the AND and OR query operations and the range of query conditions. All experimental results are based on relative errors. Moreover, the number of quasi-



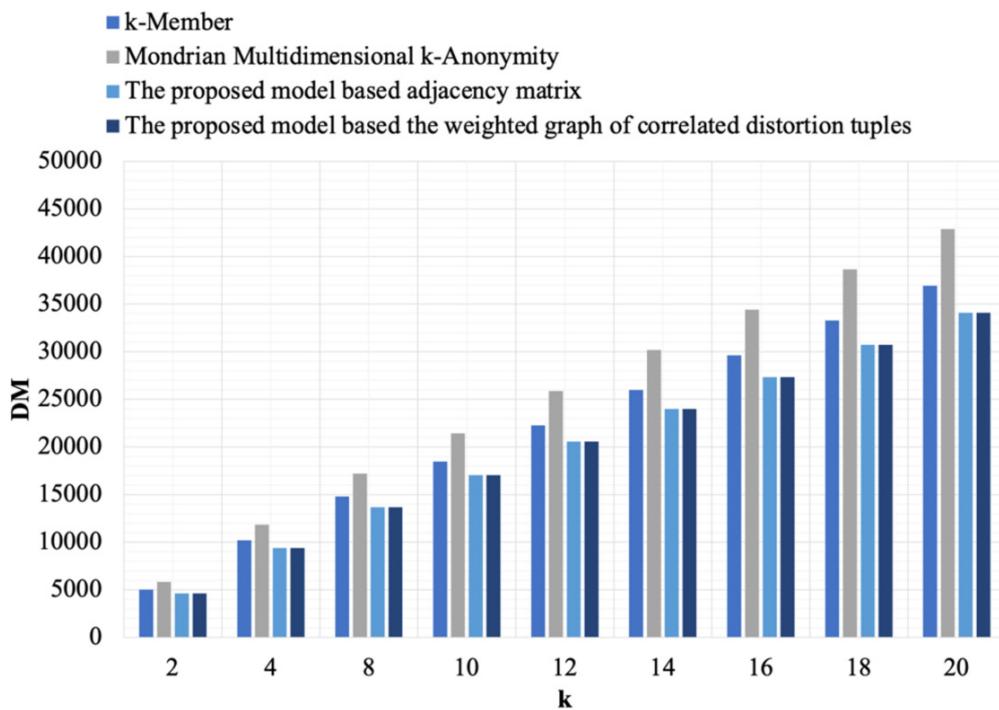
**Fig.11:** The effectiveness based on the parameter  $k$  in conjunction with PREC.



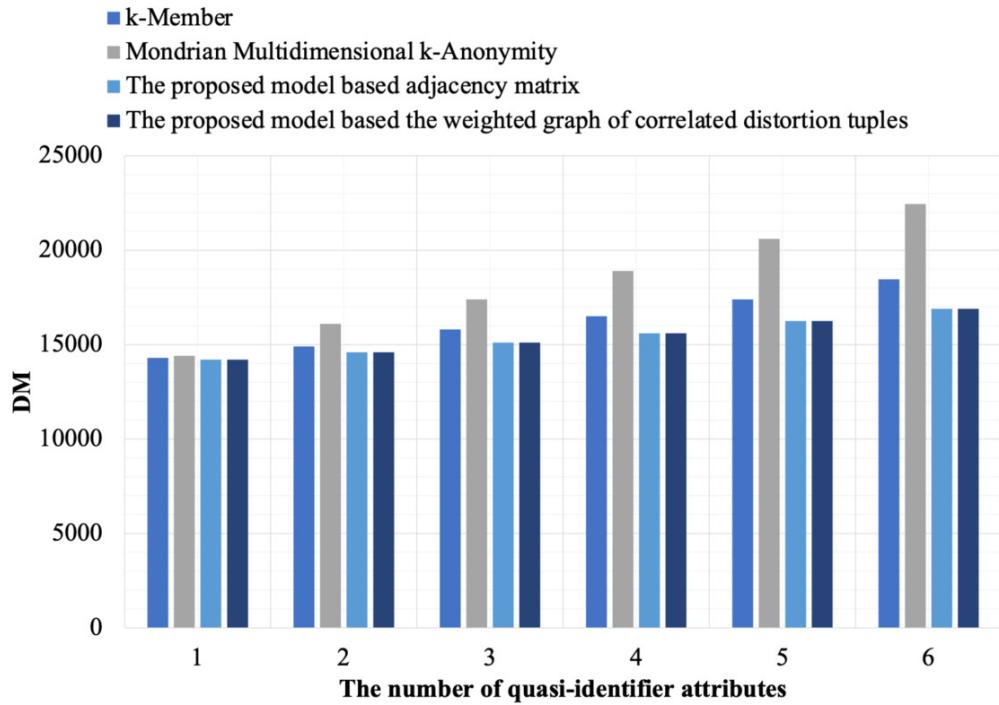
**Fig.12:** The effectiveness based on the number of quasi-identifier attributes in conjunction with PREC.



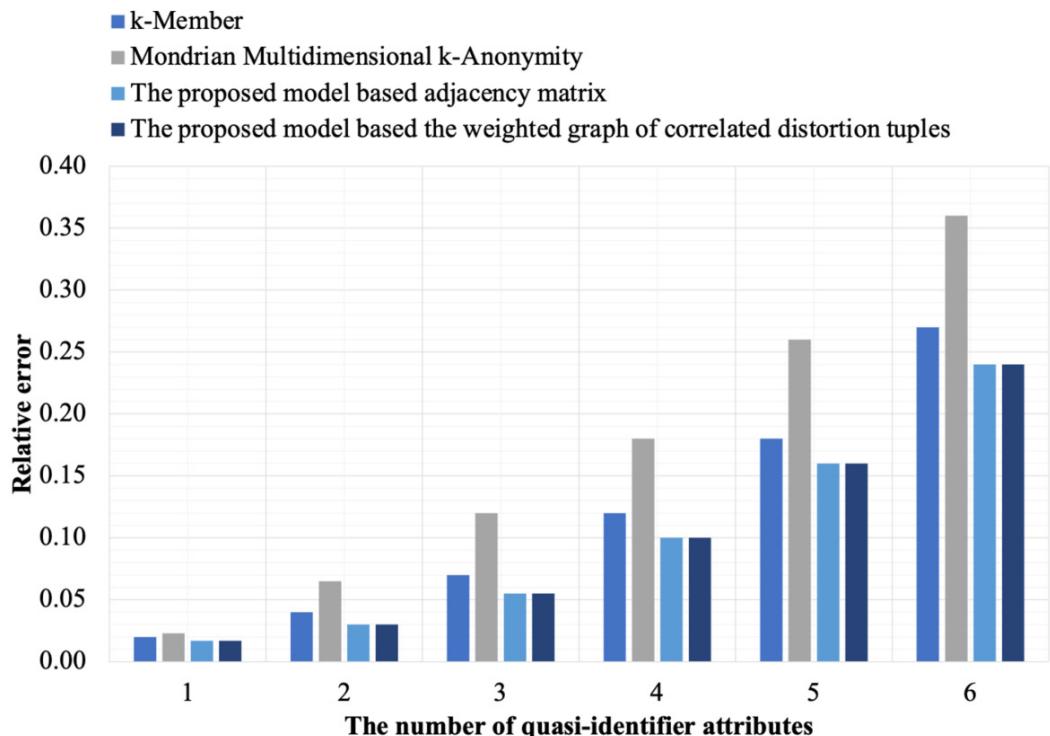
**Fig.13:** The effectiveness based on the size of datasets in conjunction with PREC.



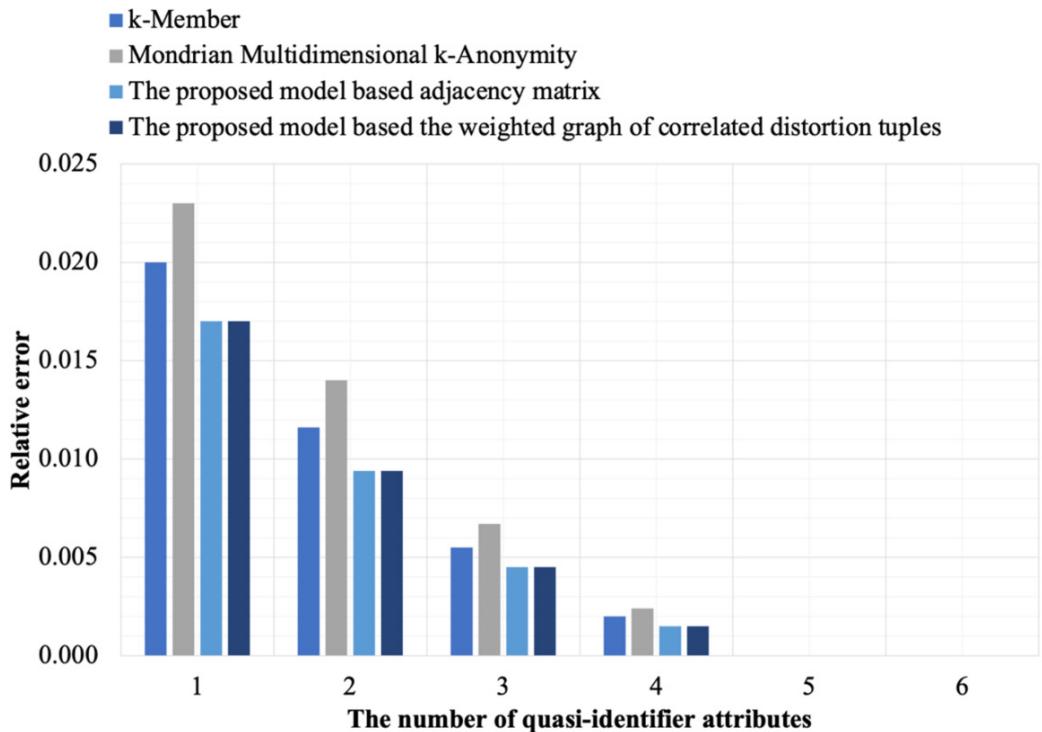
**Fig.14:** The effectiveness based on the parameter k in conjunction with DM.



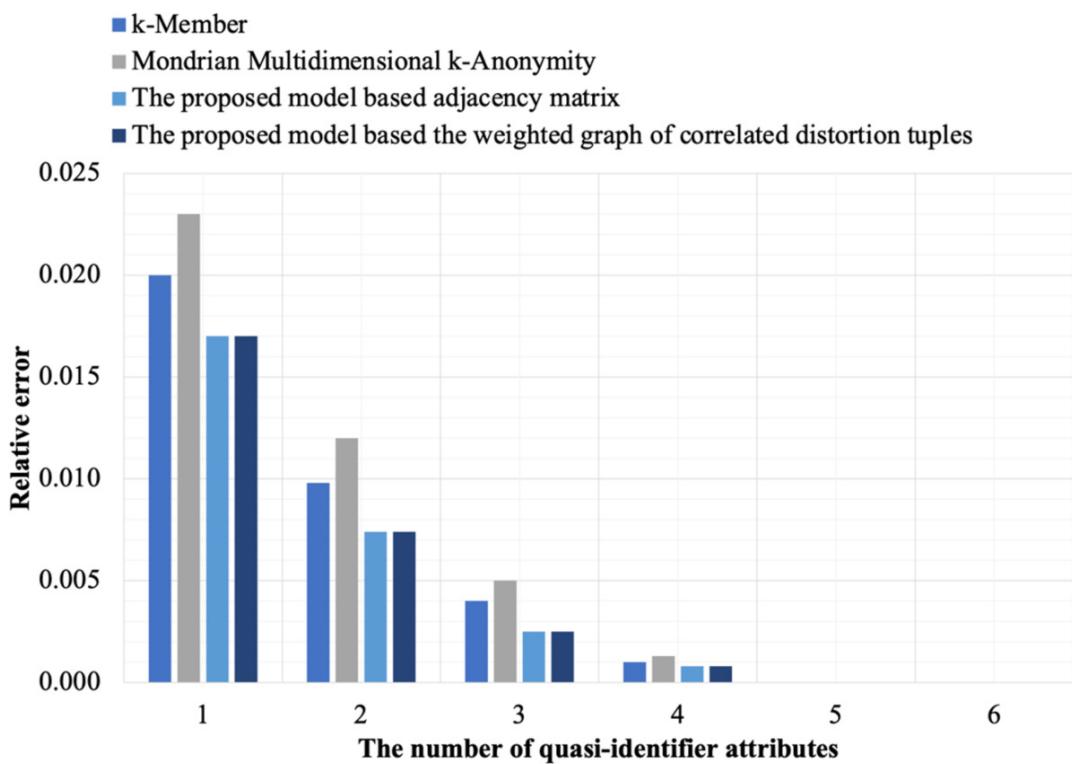
**Fig.15:** The effectiveness based on the number of quasi-identifier attributes in conjunction with DM.



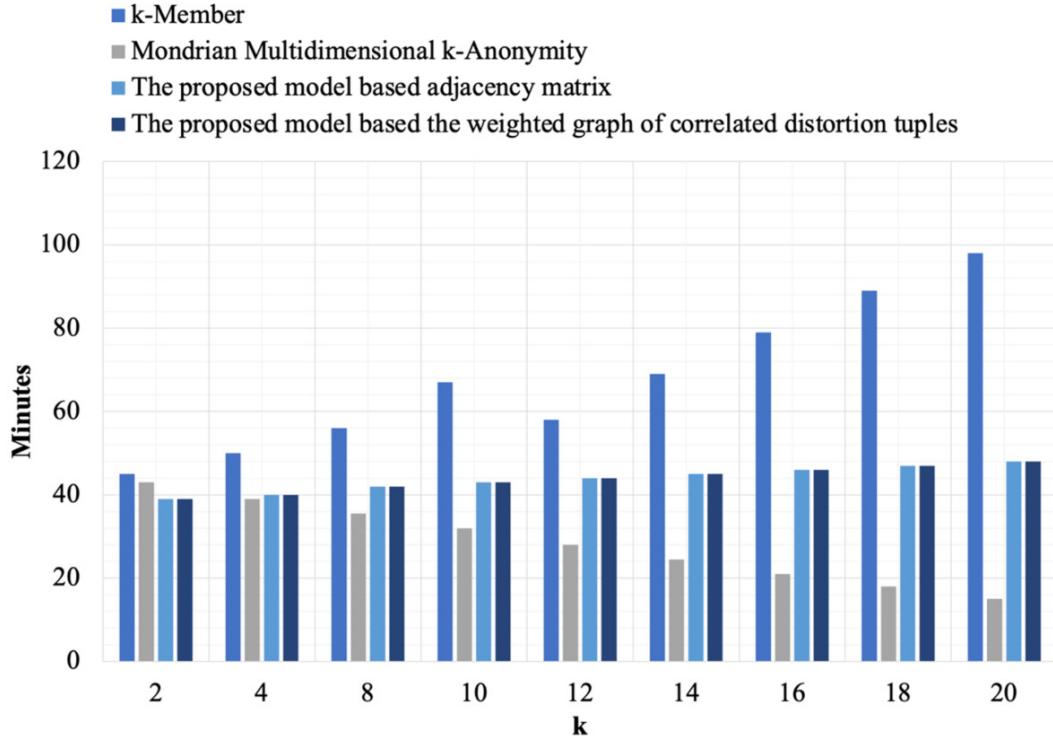
**Fig.16:** The effectiveness based on the AND query operation in conjunction with relative errors.



*Fig.17:* The effectiveness based on the OR query in conjunction with relative errors.



*Fig.18:* The effectiveness based on the range of queries in conjunction with relative errors.



**Fig. 19:** Execution time.

identifier attributes in queried conditions is varied from 1 to 6.

From the experimental results shown in Figures 16, 17, and 18, the number of quasi-identifier attributes is more influential to the query results. With the AND operation, Figure 16, we can see that the number of condition attributes has more effect on the penalty of query results, i.e., when the number of condition attributes is increased, the quality of query results is decreased. This effect of query results is the limitation of the distortion options that all experimental privacy preservation models have. When the number of condition attributes increases, the satisfied values for constructing the query results are more different from the original. Contrastively, when the number of condition attributes increases, the quality of query results of the OR query operations and the range of query conditions are increased (they are shown in Figures 17 and 18). This is because when the number of condition attributes is increased, the satisfied values of the query results from the distorted datasets and their original lead are more similar.

### 5.2.2 Efficiency

In this section, the efficiency of the proposed privacy preservation models is evaluated. Moreover, all tuples and all attributes are available in the experiments. The value of  $k$  is varied from 2 to 20. From the experimental results shown in Figure 19, we can see that when the value of  $k$  is increased, the execution time for choosing the suitable tuples to construct the

equivalence classes of the proposed technique and  $k$ -member is also increased. That is because the higher value of  $k$  leads to the larger size of the equivalence classes in datasets. Thus, the number of iterations for constructing the equivalence classes of datasets is increased. However, both proposed privacy preservation models are more efficient than  $k$ -member. In addition, the value of  $k$  is 10. We can see that  $k$ -member uses the execution time for constructing its released datasets to be more than when  $k$  is set to be 11 because  $k$ -member has both sub-algorithms for considering the suitable tuples to equivalence classes, i.e., the best tuple selection algorithm and the best equivalence class selection algorithm. The best tuple selection algorithm is the main algorithm of  $k$ -member, while the best equivalence class selection algorithm is the optional algorithm of  $k$ -member. Thus, when the best equivalence class selection algorithm is enabled, the execution time of the  $k$ -member is increased. Contrastively, the trend of Mondrian Multidimensional  $k$ -anonymity uses the execution time to be different from the proposed privacy preservation models and  $k$ -member, i.e., when the number of  $k$  is increased, the execution time for constructing the released datasets of Mondrian Multidimensional  $k$ -anonymity is decreased. The cause of decreasing the execution time of Mondrian Multidimensional  $k$ -anonymity is that the search space for considering the suitable tuples for constructing the equivalence classes of datasets is reduced by half of the previous process.

## 6. CONCLUSION

In this work, both privacy preservation models can transform datasets for satisfying  $k$ -anonymity constraints to be proposed. They are based on the weighted graph of correlated distortion tuples and the adjacency matrix of tuple distances. That is, every equivalence class of datasets is constructed from the group of the more similar tuples, i.e., the group of tuples has the summation of distance tuples to be minimum. Moreover, all experimental results indicate that both proposed privacy preservation models are more effective and efficient than the compared privacy preservation models. In addition, the proposed privacy preservation models can be further applied in  $l$ -diversity,  $(k, e)$ -anonymous,  $(\alpha, k)$ -anonymity,  $t$ -closeness,  $k^m$ -anonymity, and LKC-privacy.

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